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**Mathematics: applications and interpretation**  
**Higher level**  
**Paper 1**

Thursday 6 May 2021 (afternoon)

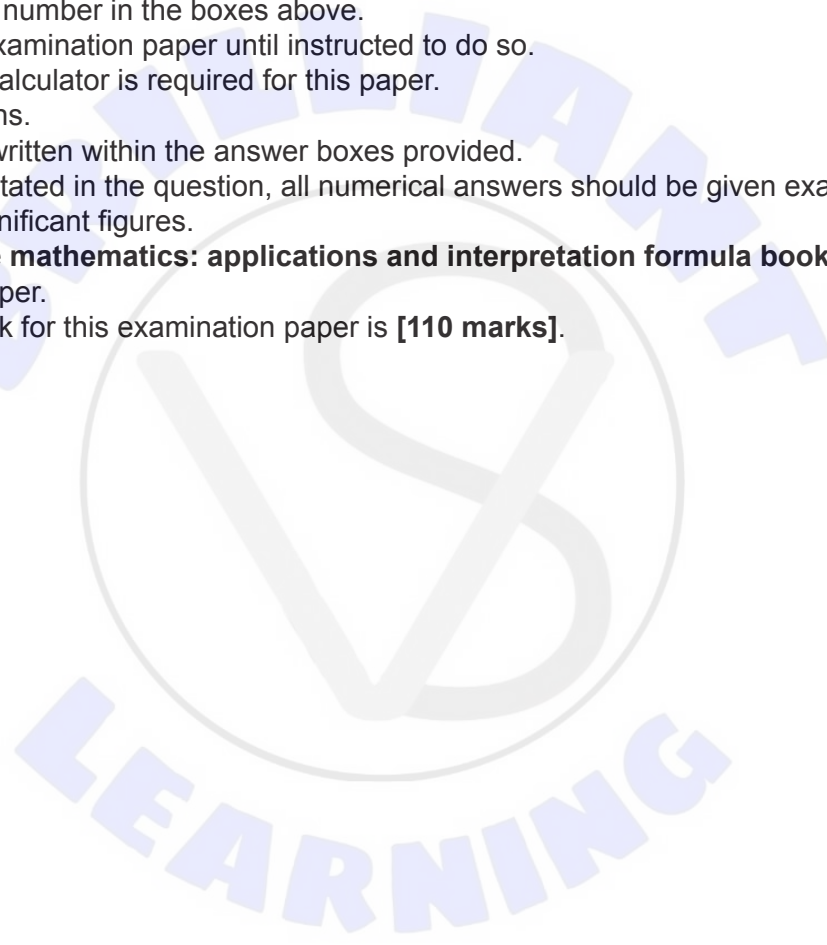
Candidate session number

2 hours

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**Instructions to candidates**

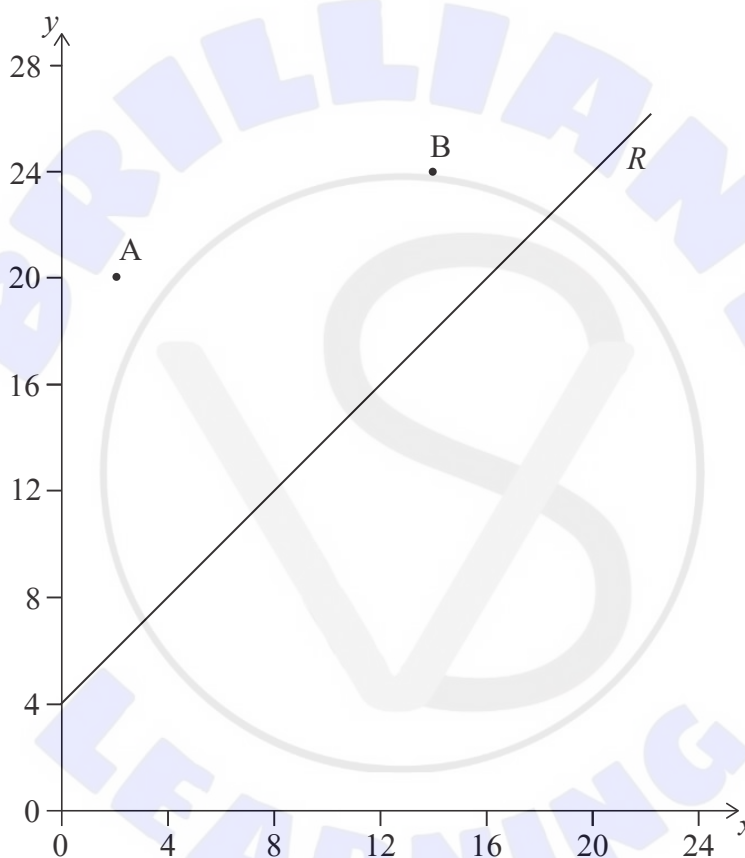
- Write your session number in the boxes above.
- Do not open this examination paper until instructed to do so.
- A graphic display calculator is required for this paper.
- Answer all questions.
- Answers must be written within the answer boxes provided.
- Unless otherwise stated in the question, all numerical answers should be given exactly or correct to three significant figures.
- A clean copy of the **mathematics: applications and interpretation formula booklet** is required for this paper.
- The maximum mark for this examination paper is **[110 marks]**.



Answers must be written within the answer boxes provided. Full marks are not necessarily awarded for a correct answer with no working. Answers must be supported by working and/or explanations. Solutions found from a graphic display calculator should be supported by suitable working. For example, if graphs are used to find a solution, you should sketch these as part of your answer. Where an answer is incorrect, some marks may be given for a correct method, provided this is shown by written working. You are therefore advised to show all working.

1. [Maximum mark: 7]

Two schools are represented by points  $A(2, 20)$  and  $B(14, 24)$  on the graph below. A road, represented by the line  $R$  with equation  $-x + y = 4$ , passes near the schools. An architect is asked to determine the location of a new bus stop on the road such that it is the same distance from the two schools.



- (a) Find the equation of the perpendicular bisector of  $[AB]$ . Give your equation in the form  $y = mx + c$ . [5]
- (b) Determine the coordinates of the point on  $R$  where the bus stop should be located. [2]

(This question continues on the following page)





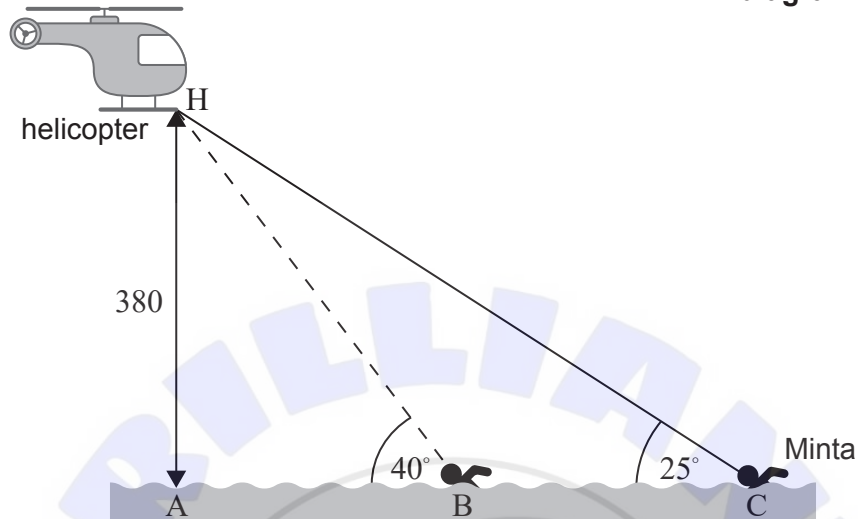




4. [Maximum mark: 6]

The diagram below shows a helicopter hovering at point H, 380m vertically above a lake. Point A is the point on the surface of the lake, directly below the helicopter.

diagram not to scale



Minta is swimming at a constant speed in the direction of point A. Minta observes the helicopter from point C as she looks upward at an angle of  $25^\circ$ . After 15 minutes, Minta is at point B and she observes the same helicopter at an angle of  $40^\circ$ .

- (a) Find the distance from A to C. [2]
- (b) Find the distance from B to C. [3]
- (c) Find Minta's speed, in metres per hour. [1]

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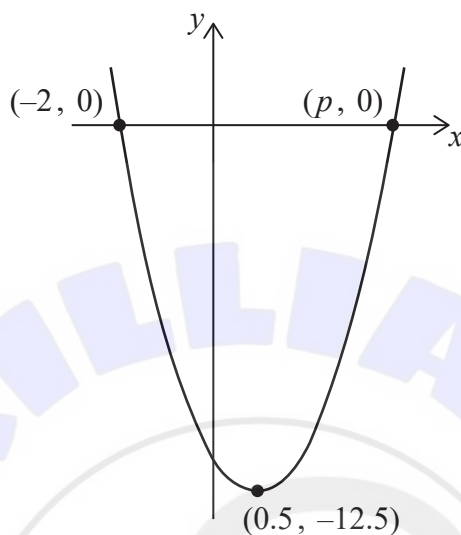




## 6. [Maximum mark: 7]

Consider the function  $f(x) = ax^2 + bx + c$ . The graph of  $y = f(x)$  is shown in the diagram. The vertex of the graph has coordinates  $(0.5, -12.5)$ . The graph intersects the  $x$ -axis at two points,  $(-2, 0)$  and  $(p, 0)$ .

diagram not to scale



- (a) Find the value of  $p$ . [1]
- (b) Find the value of
- (i)  $a$ .
  - (ii)  $b$ .
  - (iii)  $c$ . [5]
- (c) Write down the equation of the axis of symmetry of the graph. [1]

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13. [Maximum mark: 8]

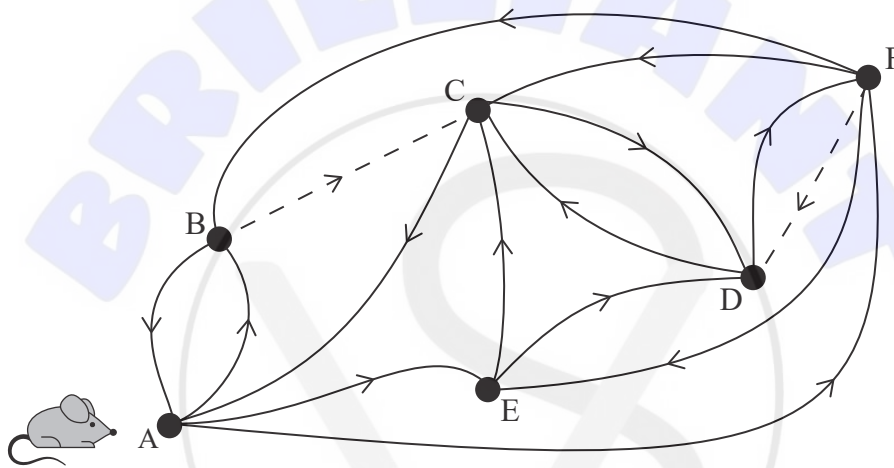
The graph below shows a small maze, in the form of a network of directed routes. The vertices A to F show junctions in the maze and the edges show the possible paths available from one vertex to another.

A mouse is placed at vertex A and left to wander the maze freely. The routes shown by dashed lines indicate paths sprinkled with sugar.

When the mouse reaches any junction, she rests for a constant time before continuing.

At any junction, it may also be assumed that

- the mouse chooses any available normal path with equal probability
- if the junction includes a path sprinkled with sugar, the probability of choosing this path is twice that of a normal path.



- (a) Determine the transition matrix for this graph. [3]
- (b) If the mouse was left to wander indefinitely, use your graphic display calculator to estimate the percentage of time that the mouse would spend at point F. [3]
- (c) Comment on your answer to part (b), referring to at least one limitation of the model. [2]

(This question continues on the following page)









