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Mathematics: applications and interpretation
Standard level
Paper 1

Thursday 6 May 2021 (afternoon)

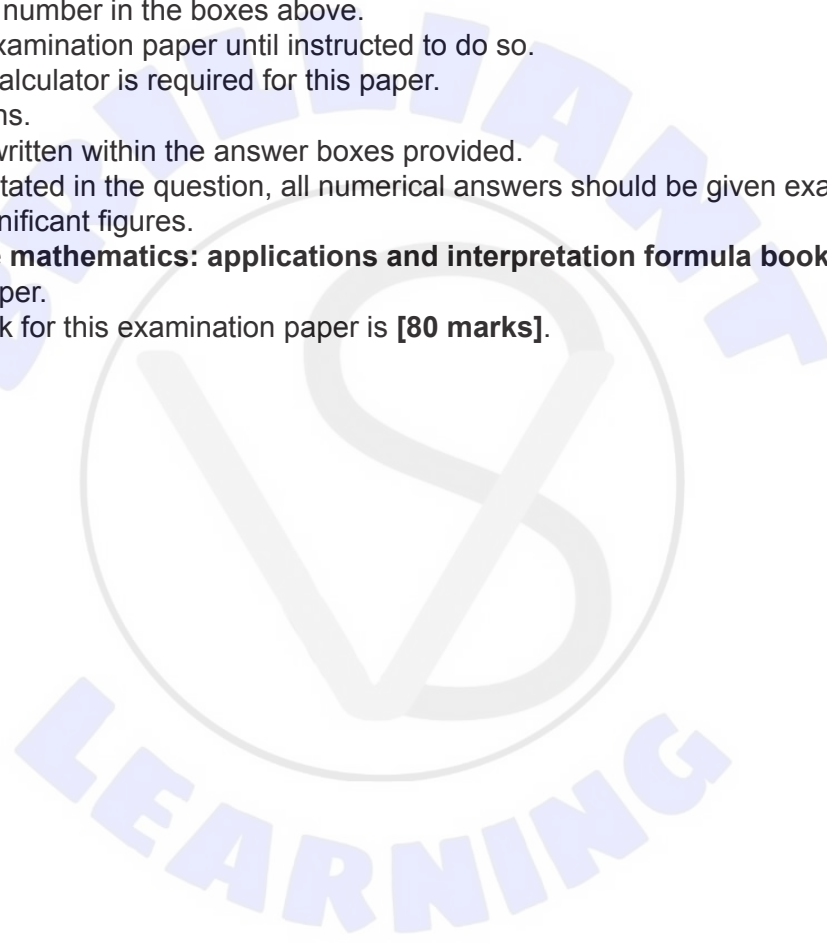
Candidate session number

1 hour 30 minutes

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Instructions to candidates

- Write your session number in the boxes above.
- Do not open this examination paper until instructed to do so.
- A graphic display calculator is required for this paper.
- Answer all questions.
- Answers must be written within the answer boxes provided.
- Unless otherwise stated in the question, all numerical answers should be given exactly or correct to three significant figures.
- A clean copy of the **mathematics: applications and interpretation formula booklet** is required for this paper.
- The maximum mark for this examination paper is **[80 marks]**.

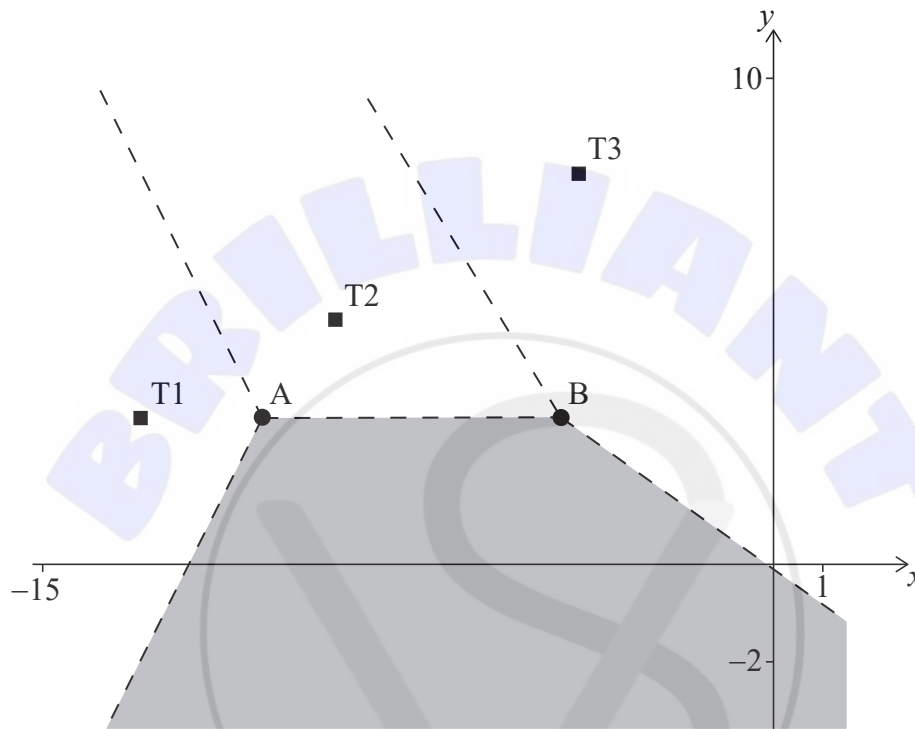


5. [Maximum mark: 6]

The Voronoi diagram below shows three identical cellular phone towers, T1, T2 and T3. A fourth cellular phone tower, T4 is located in the shaded region. The dashed lines in the diagram below represent the edges in the Voronoi diagram.

Horizontal scale: 1 unit represents 1 km.

Vertical scale: 1 unit represents 1 km.



Tim stands inside the shaded region.

(a) Explain why Tim will receive the strongest signal from tower T4. [1]

Tower T2 has coordinates $(-9, 5)$ and the edge connecting vertices A and B has equation $y = 3$.

(b) Write down the coordinates of tower T4. [2]

Tower T1 has coordinates $(-13, 3)$.

(c) Find the gradient of the edge of the Voronoi diagram between towers T1 and T2. [3]

(This question continues on the following page)



8. [Maximum mark: 8]

Charlie and Daniella each began a fitness programme. On day one, they both ran 500 m. On each subsequent day, Charlie ran 100 m more than the previous day whereas Daniella increased her distance by 2% of the distance ran on the previous day.

(a) Calculate how far

(i) Charlie ran on day 20 of his fitness programme.

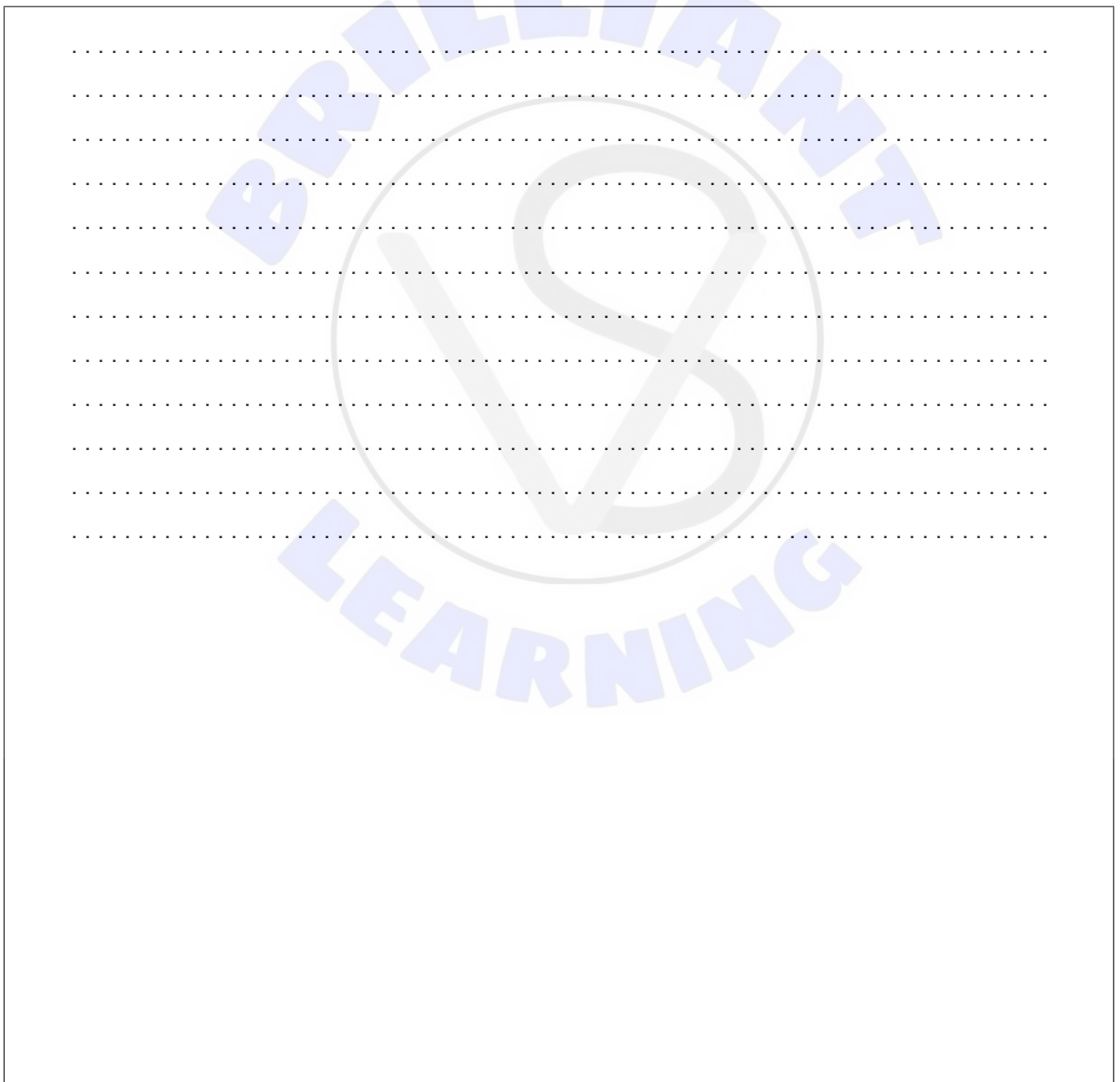
(ii) Daniella ran on day 20 of her fitness programme.

[5]

On day n of the fitness programmes Daniella runs more than Charlie for the first time.

(b) Find the value of n .

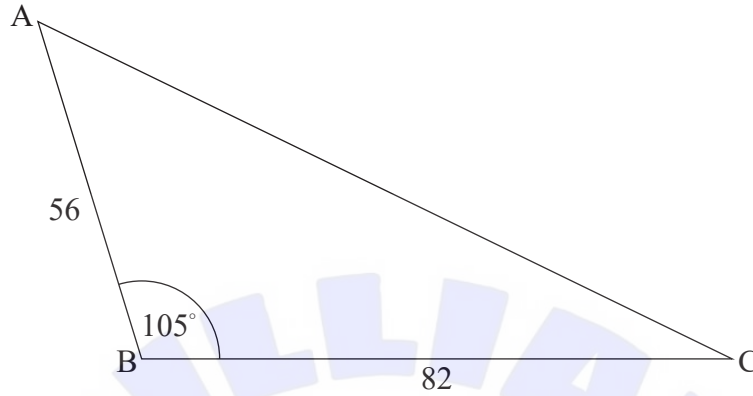
[3]



9. [Maximum mark: 5]

A triangular field ABC is such that $AB = 56\text{ m}$ and $BC = 82\text{ m}$, each measured correct to the nearest metre, and the angle at B is equal to 105° , measured correct to the nearest 5° .

diagram not to scale



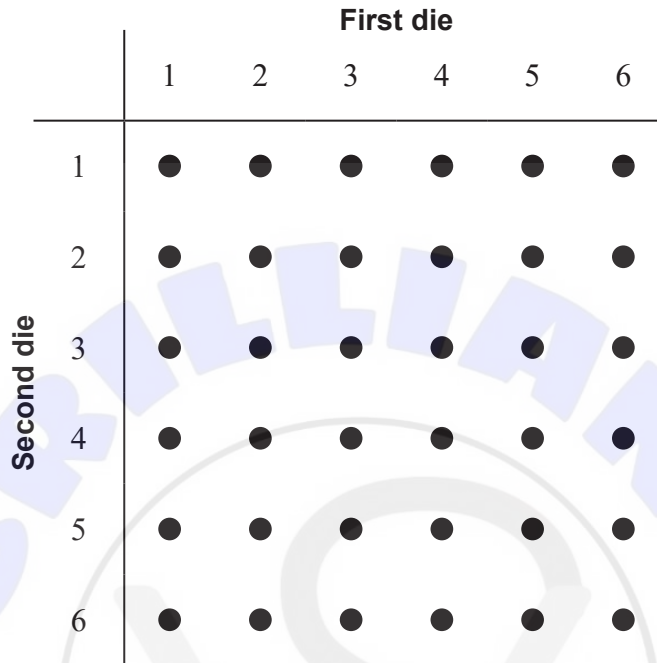
Calculate the maximum possible area of the field.

A large rectangular area containing horizontal dotted lines for writing the answer. A large, faint watermark reading 'BRILLIANT LEARNING' is visible in the background of this area.



10. [Maximum mark: 7]

A game is played where two unbiased dice are rolled and the score in the game is the greater of the two numbers shown. If the two numbers are the same, then the score in the game is the number shown on one of the dice. A diagram showing the possible outcomes is given below.



Let T be the random variable “the score in a game”.

(a) Complete the table to show the probability distribution of T . [2]

t	1	2	3	4	5	6
$P(T=t)$						

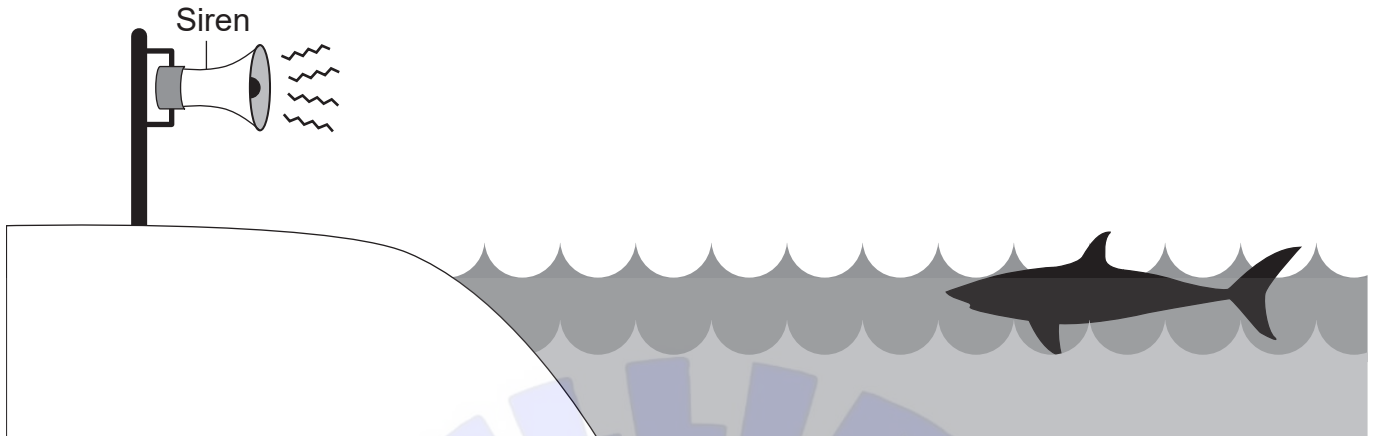
- (b) Find the probability that
- (i) a player scores at least 3 in a game.
 - (ii) a player scores 6, given that they scored at least 3. [3]
- (c) Find the expected score of a game. [2]

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11. [Maximum mark: 6]

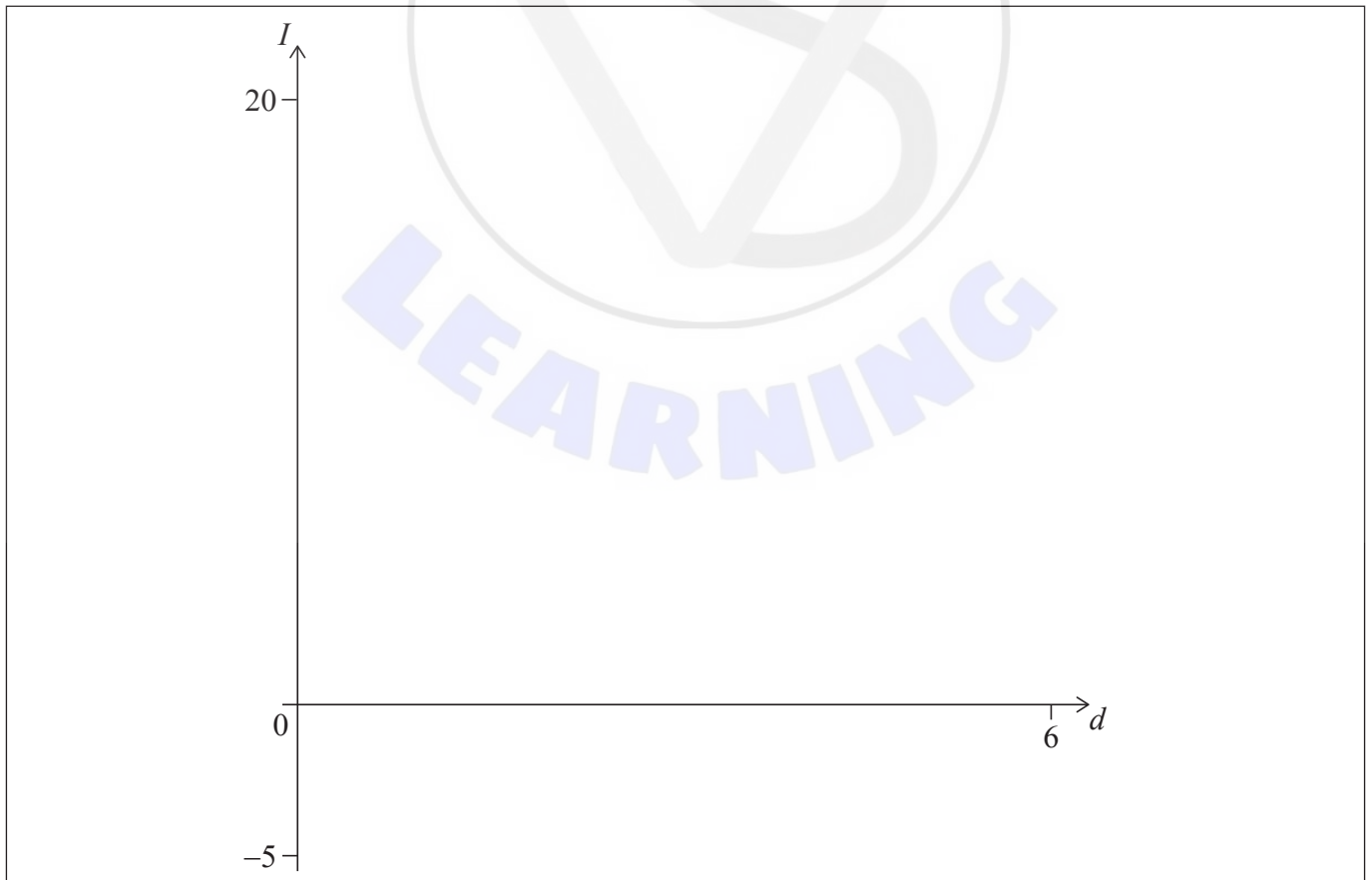
If a shark is spotted near to Brighton beach, a lifeguard will activate a siren to warn swimmers.



The sound intensity, I , of the siren varies inversely with the square of the distance, d , from the siren, where $d > 0$.

It is known that at a distance of 1.5 metres from the siren, the sound intensity is 4 watts per square metre (W m^{-2}).

- (a) Show that $I = \frac{9}{d^2}$. [2]
- (b) Sketch the curve of I on the axes below showing clearly the point (1.5, 4). [2]



(This question continues on the following page)

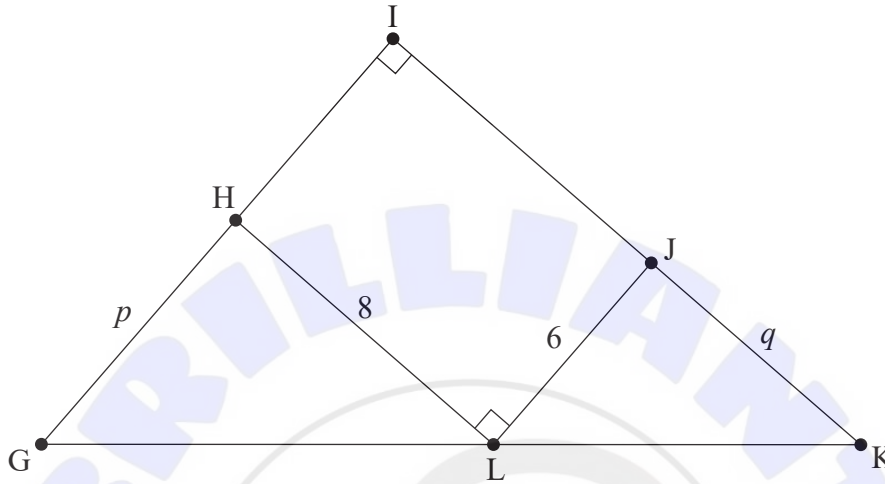


12. [Maximum mark: 8]

Ellis designs a gift box. The top of the gift box is in the shape of a right-angled triangle GIK.

A rectangular section HIJL is inscribed inside this triangle. The lengths of GH, JK, HL, and LJ are p cm, q cm, 8 cm and 6 cm respectively.

diagram not to scale



The area of the top of the gift box is A cm².

(a) (i) Find A in terms of p and q .

(ii) Show that $A = \frac{192}{q} + 3q + 48$.

[4]

(b) Find $\frac{dA}{dq}$.

[2]

Ellis wishes to find the value of q that will minimize the area of the top of the gift box.

(c) (i) Write down an equation Ellis could solve to find this value of q .

(ii) Hence, or otherwise, find this value of q .

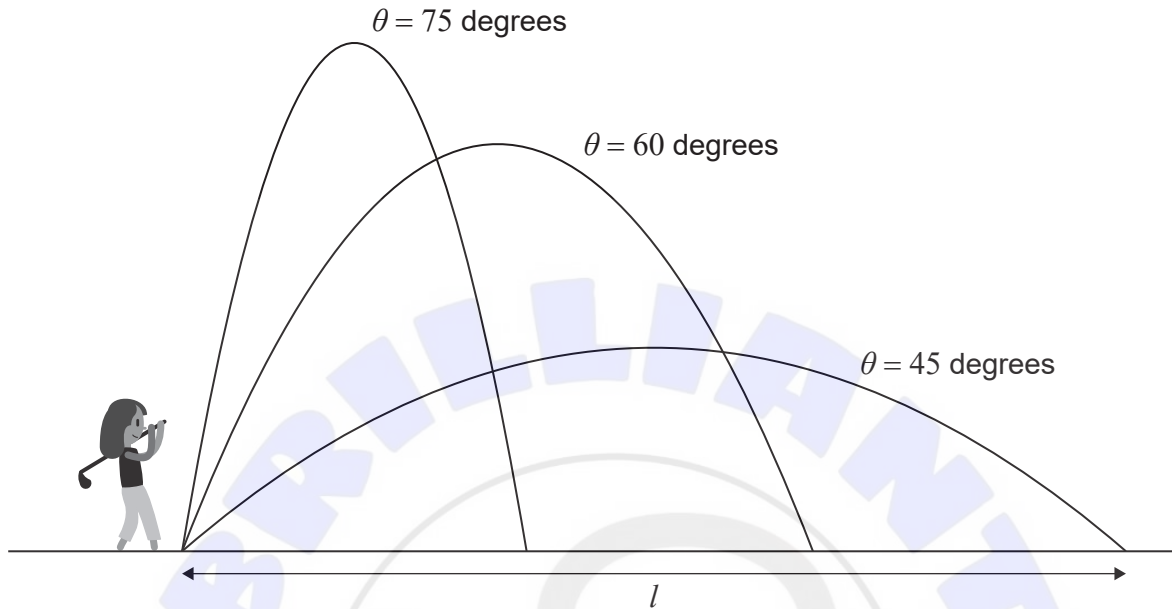
[2]

(This question continues on the following page)



13. [Maximum mark: 8]

Sieun hits golf balls into the air. Each time she hits a ball she records θ , the angle at which the ball is launched into the air, and l , the horizontal distance, in metres, which the ball travels from the point of contact to the first time it lands. The diagram below represents this information.



Sieun analyses her results and concludes:

$$\frac{dl}{d\theta} = -0.2\theta + 9, \quad 35^\circ \leq \theta \leq 75^\circ.$$

- (a) Determine whether the graph of l against θ is increasing or decreasing at $\theta = 50^\circ$. [3]

Sieun observes that when the angle is 40° , the ball will travel a horizontal distance of 205.5 m.

- (b) Find an expression for the function $l(\theta)$. [5]

(This question continues on the following page)





Please **do not** write on this page.

Answers written on this page
will not be marked.

